# Bayesian Atmospheric Tomography for Detection and Estimation of Methane Emissions

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## Motivation & Background

- Methane (CH<sub>4</sub>) and carbon dioxide (CO<sub>2</sub>) are the most prevalent anthropogenic greenhouse gases (GHGs) in the atmosphere.
- A major portion of the UNFCCC Paris Agreement is dedicated to the reduction of GHG emissions.
- While there have been substantial advances in the detection and measurement of GHG emissions, quantifying these emissions remains a predominantly open problem.

## Motivation & Background



Figure 1: Simplified schematic of the global  $CO_2$  cycle. Figure sourced from IPCC (2014).



## Ginninderra Experiment

In 2015, a controlled-release experiment headed by Geoscience Australia was conducted at the Ginninderra Controlled Release Facility near Canberra.

Two methane release rate periods:

- 5.8 g min<sup>-1</sup> between April 23 and June 7 (excluding May 26 and May 27);
- 5.0 g min<sup>-1</sup> between June 8 and June 12.

**Aim:** To develop methodology which can recover a range of plausible values for the emission rate irrespective of the specific type of instruments used.

### Ginninderra Experiment



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### Ginninderra Experiment



We model the dispersion of methane from the source via a Gaussian plume dispersion model:

$$C(x_i, y_i, z_i, Q, U_i, H) = \frac{Q}{2\pi U_i \sigma_{y_i, k_i} \sigma_{z_i, k_i}} \exp\left(-\frac{y_i^2}{2\sigma_{y_i, k_i}^2}\right) \\ \times \left[\exp\left(-\frac{(z_i - H)^2}{2\sigma_{z_i, k_i}^2}\right) + \exp\left(-\frac{(z_i + H)^2}{2\sigma_{z_i, k_i}^2}\right)\right],$$

where

- $C(x_i, y_i, z_i, Q, U_i, H)$  is the concentration of methane at a point  $(x_i, y_i, z_i)$ ;
- Q is the methane release rate;
- *U<sub>i</sub>* is the *i*th wind speed;
- *H* is the height of the gas source;
- k<sub>i</sub> refers to one of six Pasquill stability classes;
- $\sigma_{z_i,k_i}$  and  $\sigma_{y_i,k_i}$  are the standard deviations of the time averaged plume concentrations in the *i*th *z* and *y* directions respectively.

(see Turner, 1994; Wark et al., 1998, for more details)

The Gaussian plume at height  $z_i = 1.5$  m, and  $k_i =$  extremely unstable.





It is noted that the coefficients of  $\sigma_{y_i,k_i}$  and  $\sigma_{z_i,k_i}$  could be off by a factor of two or more (Wark et al., 1998). This also appears to be the case with our categorisation scheme.



To alleviate the need for the analyst to choose scaling factors for  $\sigma_{y_i,k_i}$  and  $\sigma_{z_i,k_i}$ , we replace them in the plume model with  $\tilde{\sigma}_{y_i,k_i}$  and  $\tilde{\sigma}_{z_i,k_i}$ , such that

$$\tilde{\sigma}_{y_i,k_i} \equiv \omega_y \sigma_{y_i,k_i}, \quad \text{and} \quad \tilde{\sigma}_{z_i,k_i} \equiv \omega_z \sigma_{z_i,k_i},$$

where  $\omega_y$  and  $\omega_z$  are unknown, positive scaling parameters.



The Gaussian plume dispersion model is also known to be less accurate for low wind speeds (e.g., Turner, 1994), likely because the wind-speed  $U_i$  is in the denominator of the scaling coefficient.

We could simply remove data at low wind speeds (e.g., Feitz et al., 2018)??

#### However:

By the Central Limit Theorem and the Delta Method, we determine that, approximately,

$$\operatorname{Var}\left(rac{1}{U_{i}}
ight) \propto rac{1}{\mu_{U_{i}}^{4}},$$

where  $\mu_{U_i}$  is the mean wind speed over the *i*th time interval.

### Data model

Each measured methane concentration can be written as

$$\tilde{Y}_i = C_i + X_i + \varepsilon_i,$$

where

- C<sub>i</sub> is the *i*th plume-predicted concentration;
- X<sub>i</sub> is the sum of the *i*th CH<sub>4</sub> background concentration and instrument-specific bias; and
- ε<sub>i</sub> captures both the *i*th atmospheric transport model error and the *i*th measurement error (assumed to be Gaussian but not independent).

As in Zammit-Mangion et al. (2015) we estimate  $X_i$  as the 5th percentile of all the measurements from the instrument associated with the *i*th measurement.



### Data model

Each concentration corrected for background and instrument-specific bias, termed an *enhancement* and denoted by  $Y_i$ , can be written as

$$Y_i = \tilde{Y}_i - X_i = C_i + \varepsilon_i.$$

To account for the transport model error portion of variability in the  $\varepsilon_i$  terms, we take the following steps:

**1.** Introduce an auxiliary variable,  $m_i$  ( $m_i = 1, 2, ..., M$ ), where M is the total number of unique combinations of stability class and instrument type.

We consider *M* different precision parameters  $\tau_{m_i}$ , one for each combination.

### Data Model

**2.** We take the influence of low wind speeds into account by taking the precision of  $\varepsilon_i$  to be the appropriate  $\tau_{m_i}$  multiplied by  $\hat{U}_i$ , where

$$\hat{U}_i = egin{cases} U_i^4, & 0 < U_i < 1, \ 1, & U_i \geq 1. \end{cases}$$

We assume the  $\varepsilon_i$  terms follow a Gaussian distribution, such that

$$(\varepsilon_i \mid m_i) \sim \mathsf{Gau}(0, 1/(\tau_{m_i} \hat{U}_i)).$$



## Bayesian inversion

Let

- $\mathbf{Y} = (Y_1, Y_2, \dots, Y_N)'$  be the N enhancements;
- $m{ au} = ( au_{m_1}, au_{m_2}, \dots, au_{m_M})'$  be the M precision parameters; and
- $\mathbf{U} = (U_1, U_2, \dots, U_N)'$  be the N wind speeds;

and recall

- *H* is the height of the source;
- Q is the true methane release rate in g sec<sup>-1</sup>;

•  $\omega_y$  and  $\omega_z$  are the standard deviation scaling parameters. By Bayes' Rule:

$$p(Q \mid \mathbf{Y}, \mathbf{U}, H) \propto p(Q) \int_0^\infty \int_0^\infty \int_{\mathbb{R}^{M+}} p(\mathbf{Y} \mid Q, \tau, \omega_y, \omega_z, \mathbf{U}, H) \\ \times p(\tau) p(\omega_y) p(\omega_z) \, \mathrm{d}\tau \, \mathrm{d}\omega_y \, \mathrm{d}\omega_z,$$

- The posterior distribution is not of a known form, and so we cannot directly compute a posteriori estimates for Q, τ, ω<sub>y</sub>, and ω<sub>z</sub>.
- Instead we use a Metropolis-within-Gibbs Markov Chain Monte Carlo (MCMC) scheme.
- We take 60000 samples of each unknown parameter, discard the first 20000 samples as burn-in, and set a thinning factor of 10.
- We use R to perform the inversions.



### Results



## Conclusion

- We have proposed efficient and simple methodology for recovering a range of flux estimates which is able to accept different types of instruments.
- The simplicity of the Gaussian plume model used allows for predicted concentrations to be calculated in less than a second.
  - Contributes greatly to the efficiency of the inversion;
  - Flexibility to introduce uncertainty on parameters within the model itself at little to no computational cost.
- We recover all median emission-rate estimates within 36% of the true value, while all posterior 95% credible interval have a limit within 11% of the true value.



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- The discussion paper for this research is available at https://www.atmos-meas-tech-discuss.net/amt-2019-124/.
- The curated dataset used in this research is available at https://doi.org/10.26186/5cb7f14abd710.
- Code to reproduce all results in the discussion paper is available at https://github.com/LCartwright94/BayesianAT.



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